

Neutron Star Cooling in Strong Magnetic Field : Neutrino -Antineutrino Pair Emission and Direct Urca Processes

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Magnetar Neutron-Star with Strong Magnetic-Field

- 1) Very Strong Magnetic Field $B \sim 10^{14-15}$ G (surface)
 $B \sim 10^{17-19}$ G (insides)
- Normal Neutron Star $B \sim 10^{12-13}$ G

- 2) Long Spin Period

$$P = 2 \sim 12 \text{ s}$$

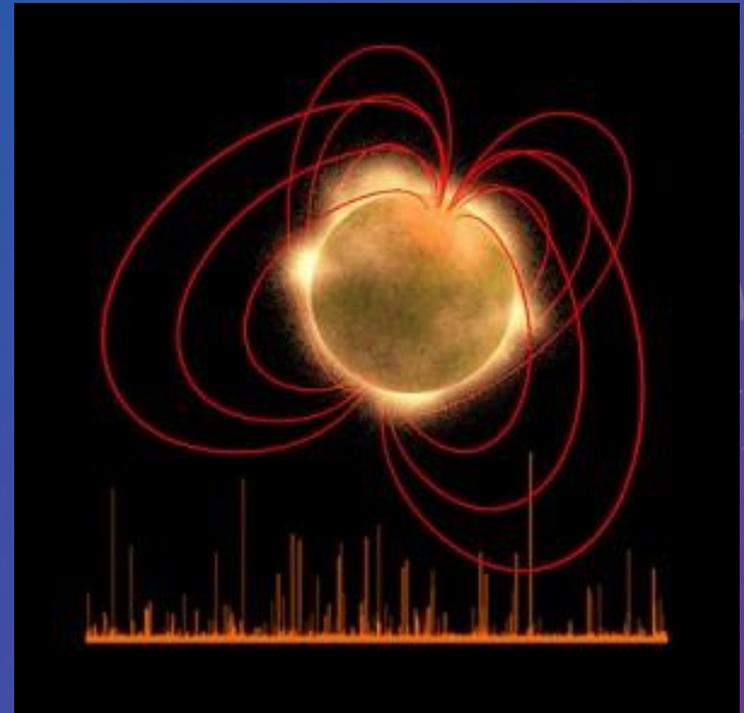
- 3) Higher Temperature

Magnetic Eng. \rightarrow Thermal Eng.

- 4) Emitting High Energy Photons

Soft Gamma Repeater (SGR)

Anomalous Xray pulsar (AXP)



Neutron Star Cooling

Neutrino Emission → Information on Inside of NSs



Neutrino Luminosity $L \propto T^8$



Proton Fraction $x_p > \frac{1}{9}$ ($k_n < k_p + k_e = 2 k_p$: Fermi Mom.)

Neutrino Luminosity $L \propto T^6$

3) neutrino-antineutrino pair emission



Conditions are determined by **Energy Momentum Conservation**

In Strong Magnetic Field

Momentum Conservation is not necessary

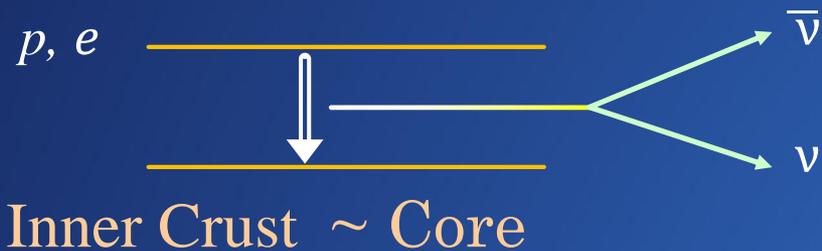
Trans. bet. Two Landau Levels give Additional Momentum

The Present Work

In Strong Magnetic Field

Transition Between Different Landau Level States

$$1) e^- \rightarrow e^- + \nu + \bar{\nu}, \quad p^+ \rightarrow p^+ + \nu + \bar{\nu} \quad (\nu\bar{\nu} - \textit{pair Emission})$$



T.M. et al., PLB805 (2020) 135413

$$2) n \rightarrow p + e^- + \bar{\nu} \quad (\textit{DU}) \quad \textit{Core}$$



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Neutron-Star Matter with Strong Mag. Field

Nucleon Mean-Fields **RMF Theory**

Magnetic Field : $\vec{B} = B\hat{z}$. $\vec{A} = (0, xB, 0)$

Dirac Eq. $\left\{ \alpha \cdot (-i\nabla - q\mathbf{A}) + \beta(M - U_s) + U_0 + \frac{e\kappa B}{2M} \right\} \psi(\mathbf{r}) = E\psi(\mathbf{r})$

U_s :Scalar Mean-Field

U_0 :Vector Mean-Field

AMM

$$BE = 16 \text{ MeV}, M_N^*/M_N = 0.70,$$
$$K = 200 \text{ MeV}, e_{sym} = 32 \text{ MeV}$$
$$\text{at } \rho_0 = 0.17 \text{ fm}^{-3}$$

Single Particle Energies and Wave-Functions

Single Particle Energy

Landau Level Number

p & e

$$E(n, p_z, s) = E^* + U_0 = \sqrt{p_z^2 + (\sqrt{2eBn} + M^{*2} + se\kappa B/2M)^2} + U_0$$

n

$$E(n, p_z, s) = E^* + U_0 = \sqrt{p_z^2 + (\sqrt{p_T^2} + M^{*2} + se\kappa B/2M)^2} + U_0,$$

Wave-Function

p & e

$$\psi_{n,s,p_z}(\mathbf{r}_1)\bar{\psi}_{n,s,p_z}(\mathbf{r}_2) = \frac{e^{i(p_y y + p_z z)}}{\sqrt{R_y R_z}} \hat{F}(x_1 - p_y/eB) \frac{\rho_M}{4E} \hat{F}(x_2 - p_y/eB)$$

$$\rho_M(n, s, P_z) = \left[E^* \gamma_0 - \zeta \sqrt{2neB} \gamma_2 - p_z \gamma_z + M^* + \frac{e\kappa B}{2M} \Sigma_z \right] \left[1 + \frac{s}{\sqrt{2neB + M^{*2}}} \left(\frac{e\kappa B}{2M} + p_z \gamma_5 \gamma^0 - E^* \gamma_5 \gamma^3 \right) \right]$$

$$\tilde{F} = \text{diag}(f_n, f_{n-1}, f_n, f_{n-1}) \quad p$$

$$= \text{diag}(f_n, f_{n-1}, f_{n-1}, f_n) \quad e$$

Neutron

$$\psi_{\mathbf{p},s}(\mathbf{r}_1)\bar{\psi}_{\mathbf{p},s}(\mathbf{r}_2) = \frac{e^{i\mathbf{p}\cdot(\mathbf{r}_1-\mathbf{r}_2)}}{\sqrt{\Omega}} \left[E^* \gamma_0 - \mathbf{p} \cdot \boldsymbol{\gamma} + M^* + \frac{e\kappa B}{2M} \Sigma_z \right] \left\{ 1 + \frac{s}{\sqrt{p_T^2 + M^{*2}}} \left[\frac{e\kappa B}{2M} + \gamma_5 (p_z \gamma^0 - E^* \gamma^3) \right] \right\}$$

Decay Width of $\nu\bar{\nu}$ - *pair Emission*

Total Luminosity

$$L_{\nu\bar{\nu}} = \frac{\pi G_F^2}{8} \sum_{n_i, s_i} \sum_{n_f, s_f} \int \frac{dp_{iz}}{2\pi} \frac{d^3 k_{iz}}{(2\pi)^3} \frac{d^3 k_{fz}}{(2\pi)^3} \frac{N_{\mu\nu} L^{\mu\nu}}{|\mathbf{k}_i| |\mathbf{k}_f| e_i e_f} (|\mathbf{k}_i| + |\mathbf{k}_f|) f(e_i) [1 - f(e_f)] \delta(e_i - e_f - |\mathbf{k}_i| - |\mathbf{k}_f|)$$

Landau Level Transition Energy is kept to be a few MeV

$$\sqrt{eB} = 2.43 \text{ MeV} \quad \text{when } B = 10^{15} \text{ G}$$

Low Temperature Expansion ($T \ll 1$)

$$f(e) = \frac{1}{1 + \exp[(e - \mu)/T]} \approx \Theta(e - \mu) + a_c T^2 \delta'(e - \mu)$$

Unavailable!

Emitted Particle Energy $\sim T$ (Temperature)

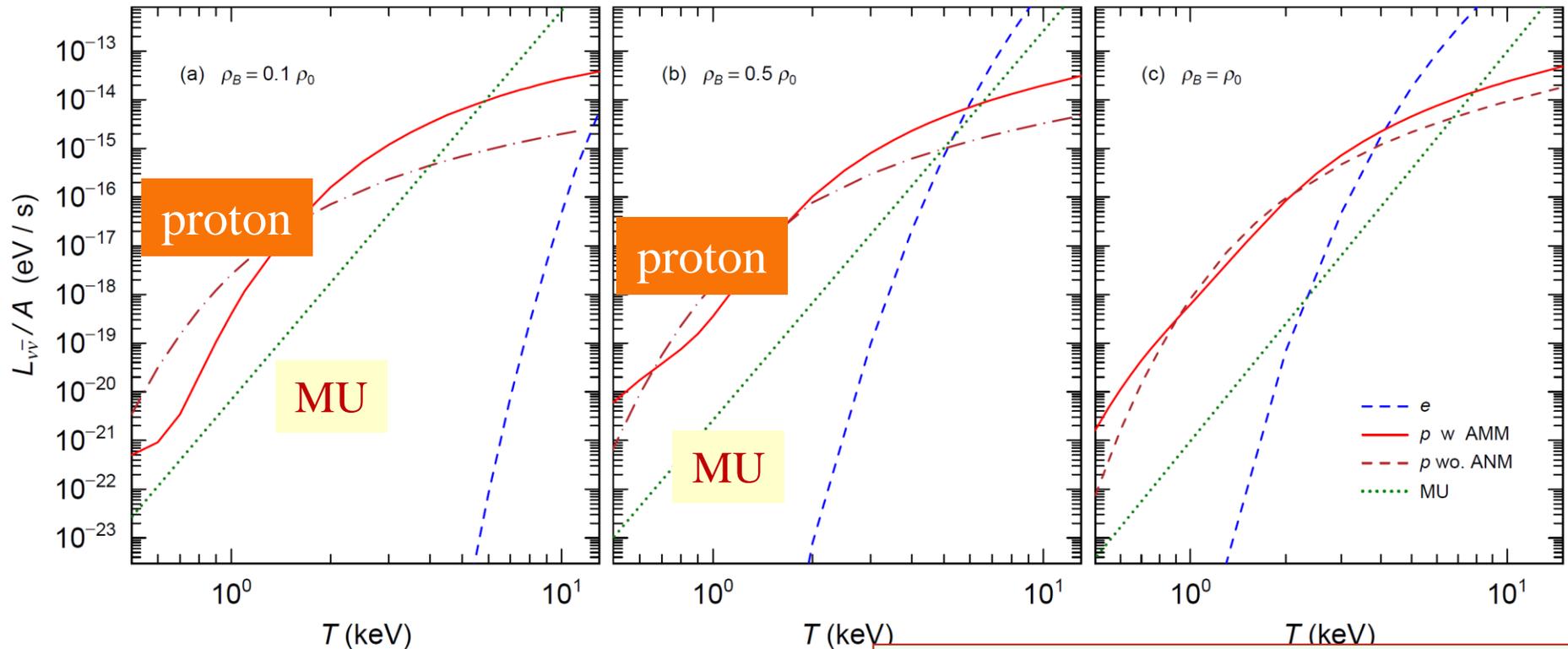
In Strong Mag. Fld. $f(e_i) \sim (1 - f(e_f)) \ll 1$

$$(e_i - e_f) \gg T$$

Neutrino Luminosity in $\nu\bar{\nu}$ - pair Emission

Temperature Dependence

$B = 10^{15}$ G



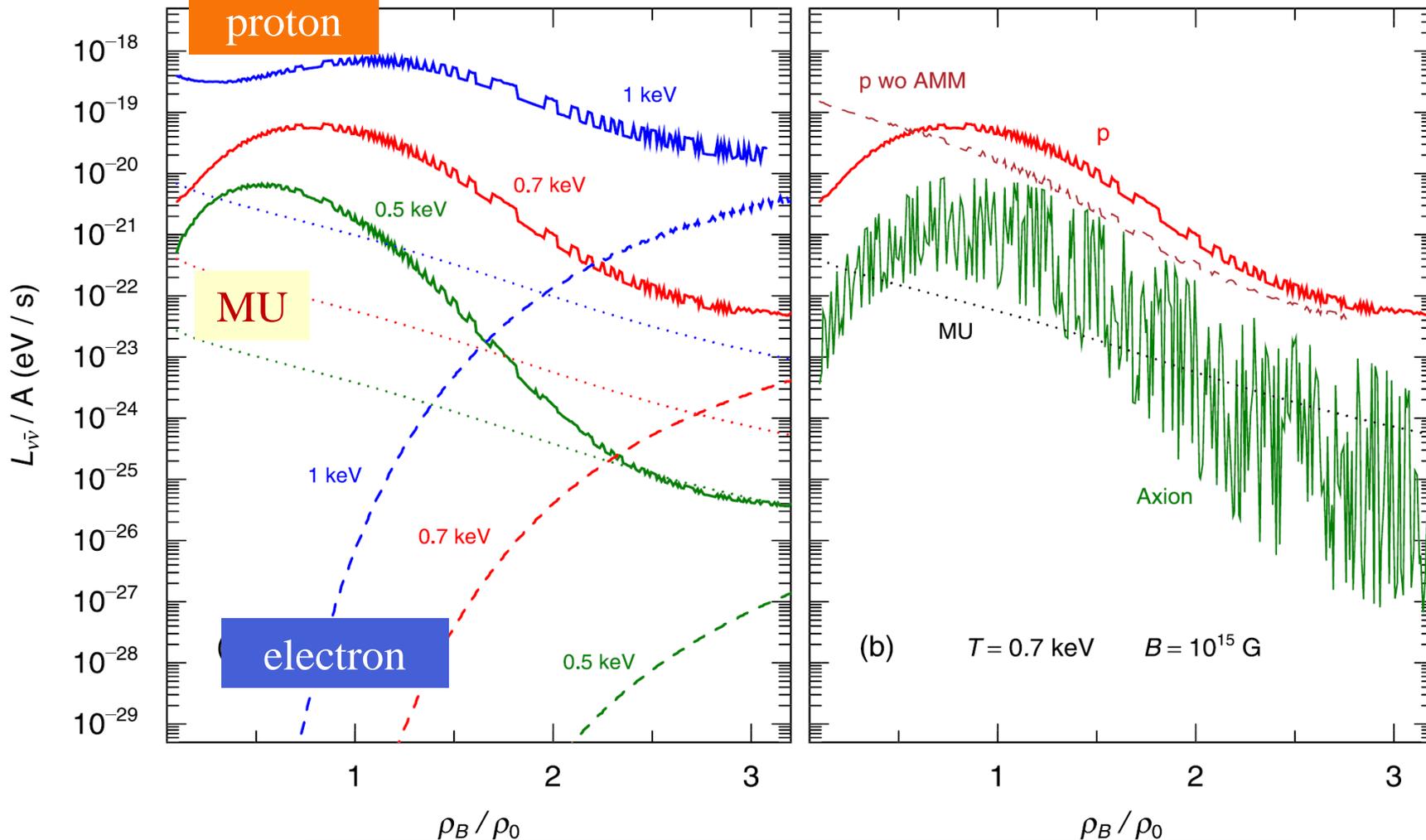
$(\nu\bar{\nu}\text{-Pair}) \gg (\text{Modified Urca})$

EOS: $BE = 16$ MeV, $M_N^*/M_N = 0.70$,

$K = 200$ MeV, $e_{sym} = 32$ MeV at $\rho_0 = 0.17$ fm $^{-3}$

Density Dependence

$\nu\bar{\nu}$ - Emissions at $B = 10^{15}$ G



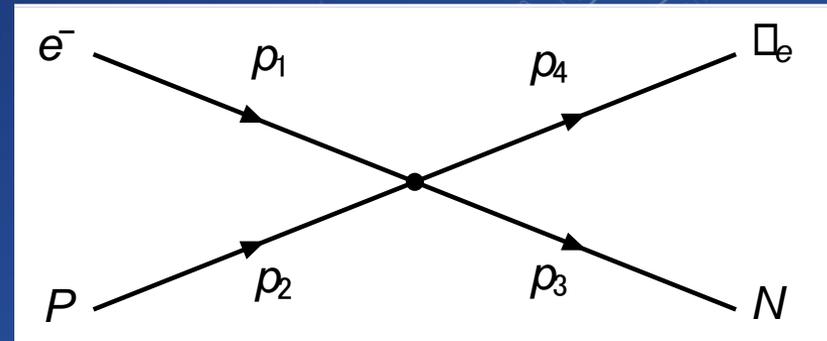
$(\nu\bar{\nu}\text{-Pair}) \gg (\text{Modified Urca})$

Effects of Magnetic Fields are Very Large

Direct Urca Process

Low Temperature Limit

$$T \rightarrow 0$$



$$e_\nu^3 n_n(E_n)[1 - n_p(E_p)]n_e(e_e) = \mathcal{I}_{DU}\delta(E_n - \mu_n)\delta(E_p - \mu_p)\delta(e_e - \mu_e).$$

$$\mathcal{I}_{DU} = \int dE_n dE_p dE_e (E_n - E_p - E_e)^3 n_n(E_n)[1 - n_p(E_p)][1 - n_e(E_e)] = \frac{457}{5040}\pi^6 T^6.$$

All Particles on Fermi Surface

Neutrino Emissivity

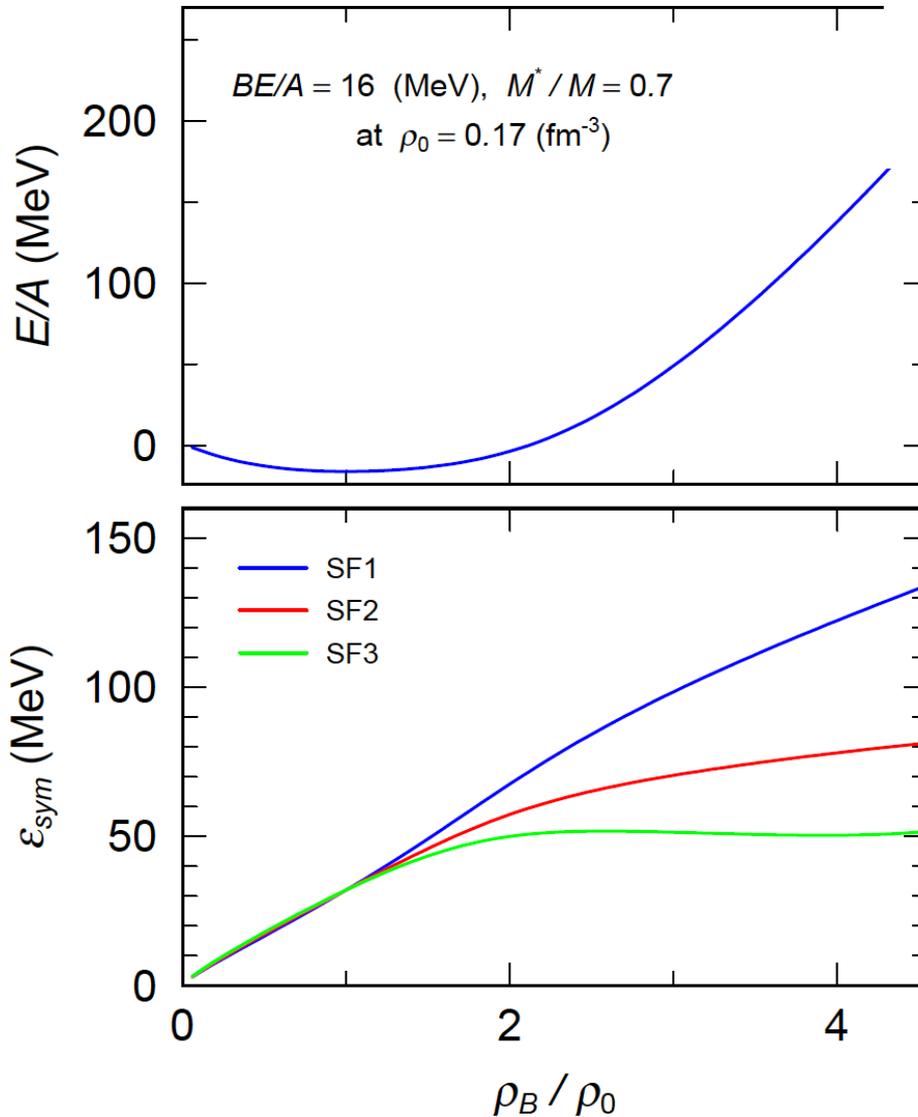
$$\epsilon_{DU} = \frac{457\pi G_F^2}{2^7 \cdot 5040} T^6 \sum_{n_e, n_p} \frac{p_{nT}}{p_{pz} p_{ez} \sqrt{p_{nT}^2 + M_n^{*2}}} \sum_s \sum_{i,j} \int \frac{d\Omega_4}{4\pi} \mathcal{M}(j_1, i_1) \mathcal{M}^*(j_2, i_2) \frac{L_{\mu\nu} N^{\mu\nu}}{e_\nu}.$$

$$\mathcal{M}(j_p, j_l) = \int dx f_{n_e+(j_l-1)/2} \left(x + \frac{p_{nT}}{\sqrt{2eB}} \right) f_{n_p+(j_p-1)/2} \left(x - \frac{p_{nT}}{\sqrt{2eB}} \right),$$

$f_n(x)$: 1 dim. HO Wave-Function

Nuclear Matter RMF Equations of State

$$\begin{aligned} \mathcal{L} = & \bar{\psi}_N(i\partial - M)\psi_N + g_\sigma\bar{\psi}_N\psi_N\sigma + g_\omega\bar{\psi}_N\gamma_\mu\psi_N\omega^\mu \\ & - \frac{C_s^{IV}}{2M^2}(\bar{\psi}_N\tau\psi_N)^2 - \frac{C_v^{IV}}{2M^2}(\bar{\psi}_N\gamma_\mu\tau\psi_N)^2 \\ & - \tilde{U}[\sigma] + \frac{1}{2}m_\omega^2\omega_\mu\omega^\mu. \end{aligned}$$



Two kinds of symmetric force

Lorenz Vector & Scalar

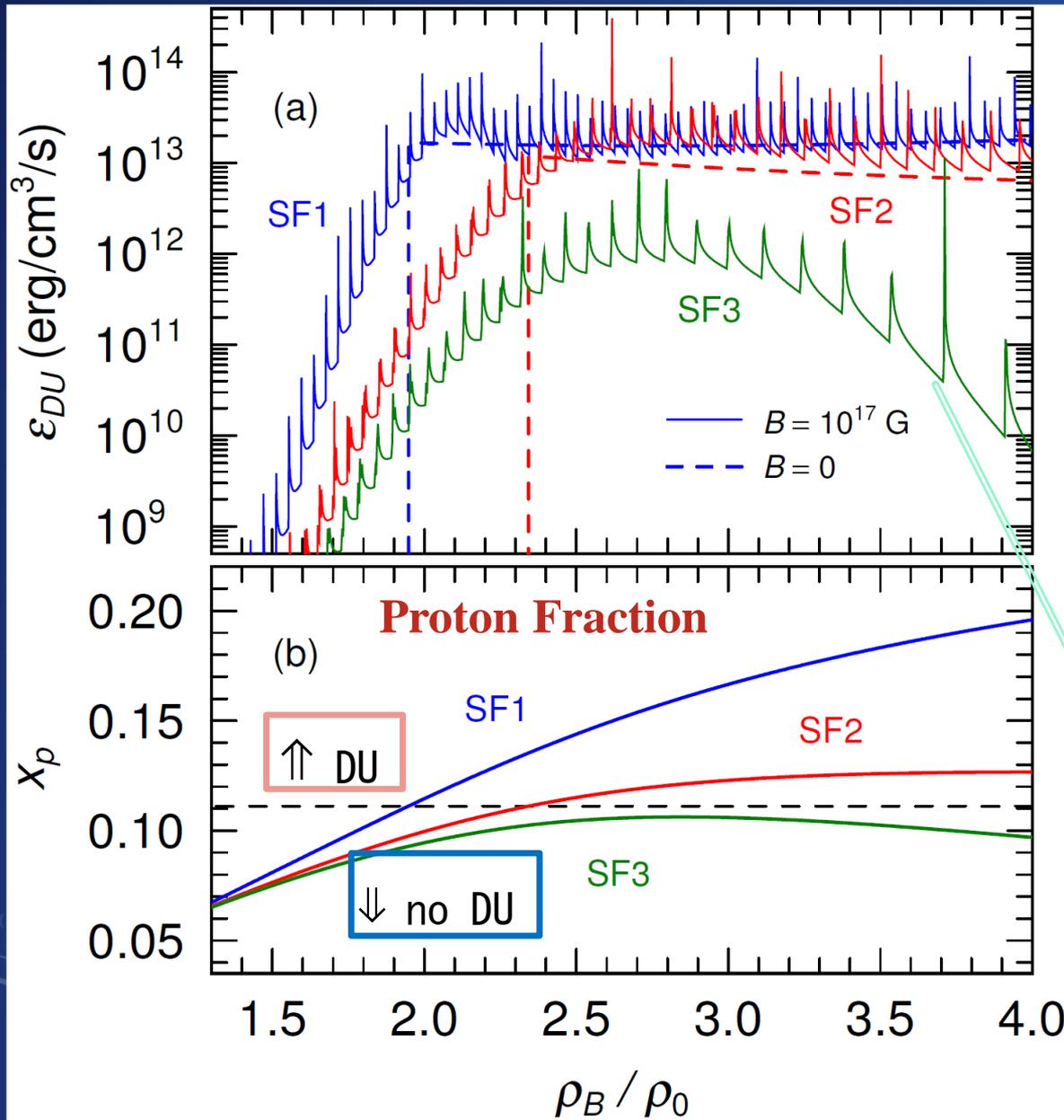
Parameter-Set	C_s^{IV}	C_v^{IV}	L (MeV)
SF1	0	20.42	92.7
SF2	23.61	0	84.1
SF3	33.02	-8.154	81.0

SF1 : Vector Type Sym. Force

SF2 : Scalar Type Sy, Force

SF3: Negative Vector

Density-Dependence of the Neutrino Emissivity in DU



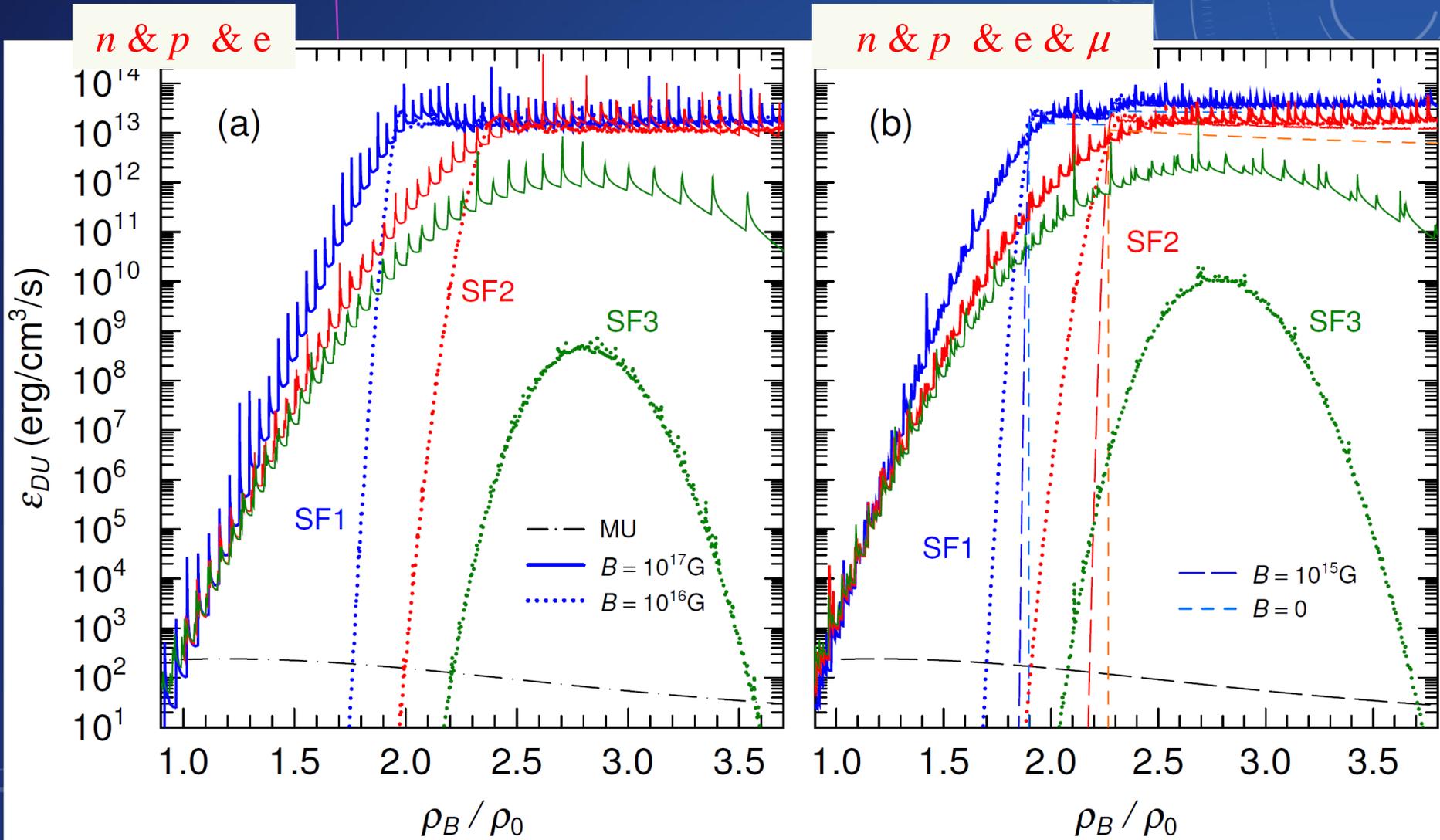
NS matter consists of
n & p & e

Spikes reflect the
density of states given
by the Landau levels

Neutrinos emitted
through Transitions
between Landau levels

DU does not appear
when $B=0$

Density & Mag. Fld. Dep. of the Neutrino Emissivity



Summary

Laudau Levels are introduced into Calculations
of Neutrino Emissions in **Strong Magnetic Field**

$\nu\bar{\nu}$ - Pair Emission

Energy Loss \gg MU

DU process from NS matter

Three Parameter-sets for Symmetry Energy

Proton Fraction \longleftrightarrow the Neutrino Emissivity.

In the forbidden region $x_p < 1/9$



Mag. Fld. make DU

At Low Temp. Limit, Mag. Effect in DU is **not very Large** when $x_p < 1/9$.

Because of Low Temperature Approximation (?) .

ν -Emissivity may become Larger in Exact Calculations

Matter include Muon Emissivity

